

# Error

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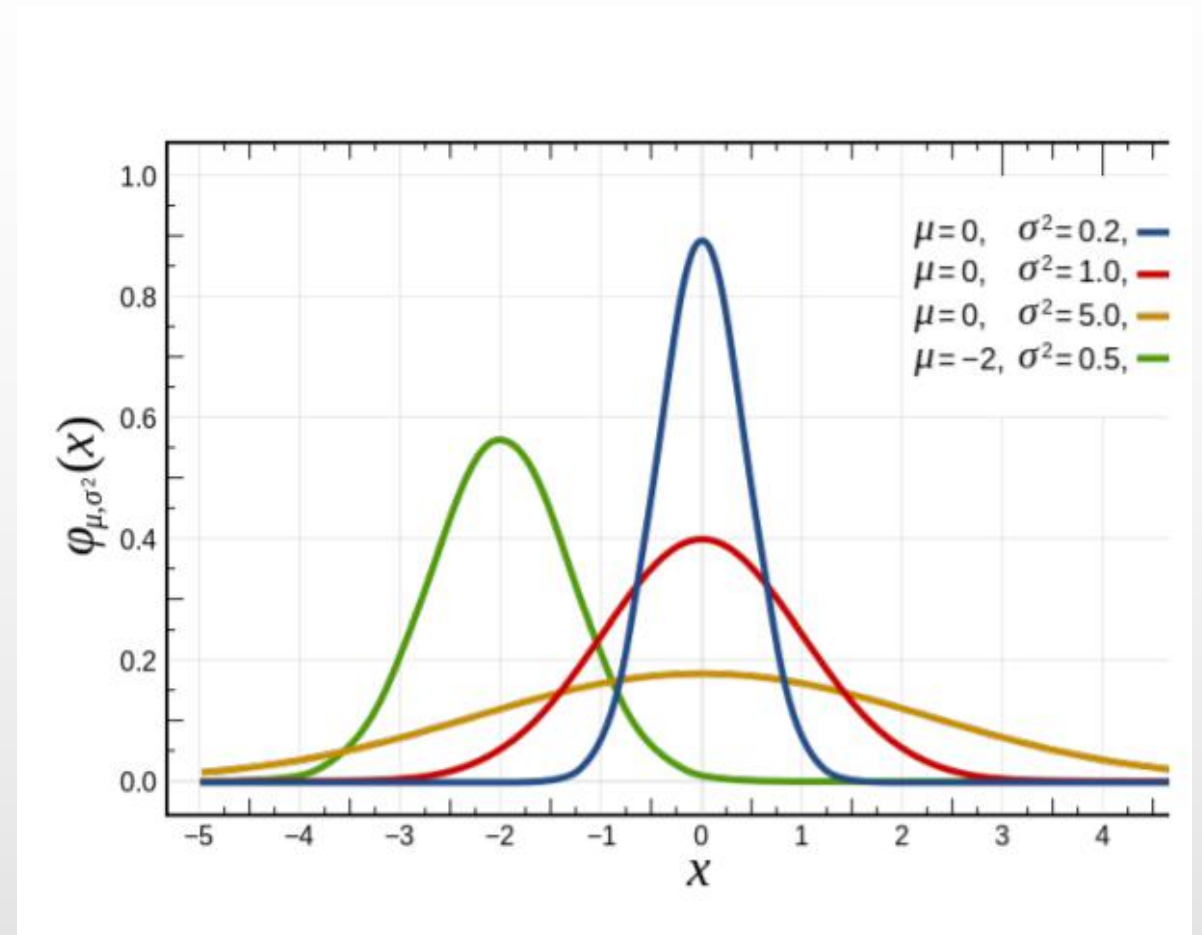
# Gaussian distribution

- $y = y_0 + \varepsilon$

- $\varepsilon \sim N(0, \sigma^2)$

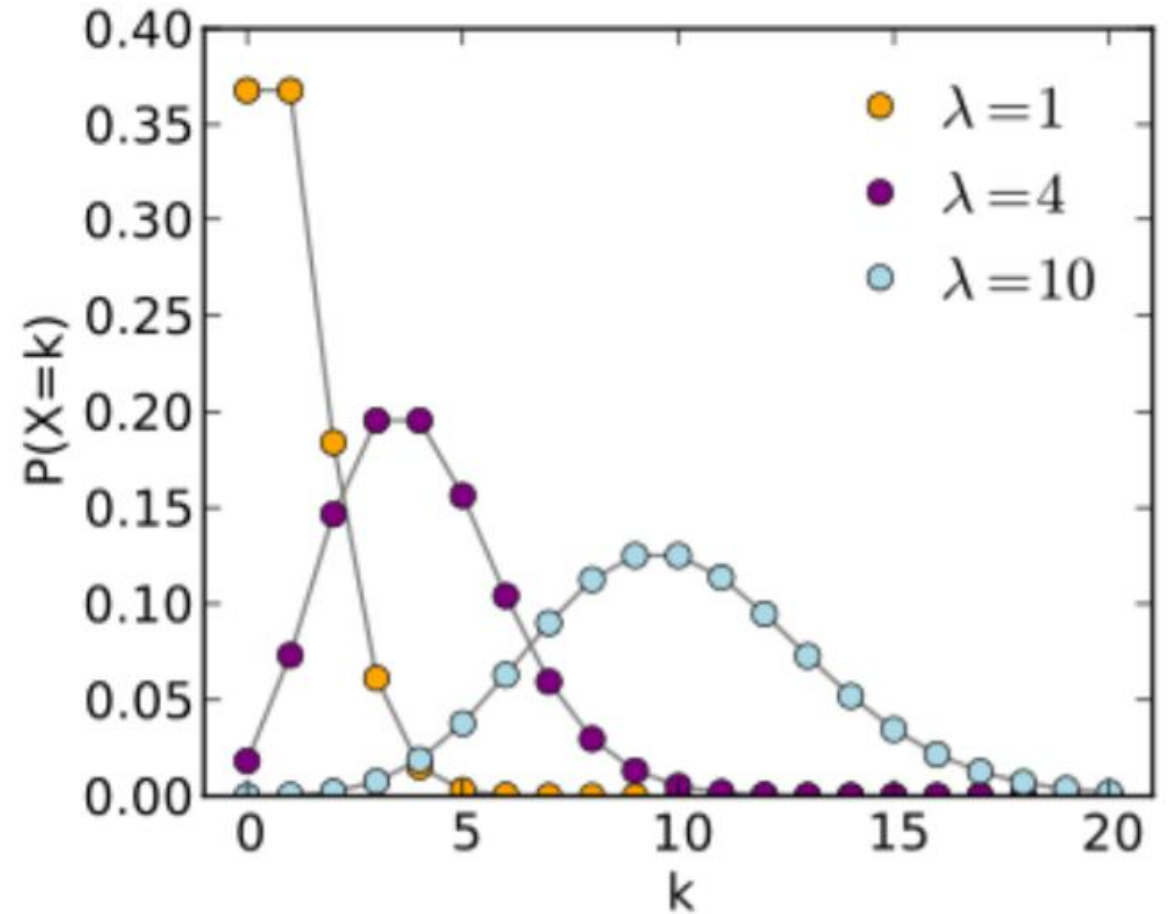
- *precision*

- *accuracy*



# Possion distribution

- $\varepsilon \sim \text{Possion}(\lambda)$
- $\lambda \leq 20$
- $\lambda \geq 20$  *Possion*  $\rightarrow$  *Normal*
- *CCD-*



# Propagation of error

$$f = aA, \quad \sigma_f^2 = a^2 \sigma_A^2$$

$$f = aA \pm bB, \quad \sigma_f^2 = a^2 \sigma_A^2 + b^2 \sigma_B^2 \pm 2ab\rho_{AB}$$

$$f = AB, \quad \sigma_f^2 \approx f^2 \left[ \left( \frac{\sigma_A}{A} \right)^2 + \left( \frac{\sigma_B}{B} \right)^2 + 2 \frac{\sigma_{AB}}{AB} \right]$$

$$f = \frac{A}{B}, \quad \sigma_f^2 \approx f^2 \left[ \left( \frac{\sigma_A}{A} \right)^2 + \left( \frac{\sigma_B}{B} \right)^2 - 2 \frac{\sigma_{AB}}{AB} \right]$$

$$f = aA^b, \quad \sigma_f^2 \approx \left( \frac{fb\sigma_A}{A} \right)^2$$

$$f = a \ln(bA), \quad \sigma_f^2 \approx \left( a \frac{\sigma_A}{A} \right)^2$$

$$f = a \log_{10}(A), \quad \sigma_f^2 \approx \left( a \frac{\sigma_A}{A \ln 10} \right)^2$$

$$f = ae^{bA}, \quad \sigma_f^2 \approx f^2 (b\sigma_A)^2$$

$$f = a^{bA}, \quad \sigma_f^2 \approx f^2 (b \ln(a) \sigma_A)^2$$

$$f = a \sin(bA), \quad \sigma_f^2 \approx (ab \cos(bA) \sigma_A)^2$$

$$f = a \cos(bA), \quad \sigma_f^2 \approx (ab \sin(bA) \sigma_A)^2$$

$$f = A^B, \quad \sigma_f^2 \approx f^2 \left[ \left( \frac{B}{A} \sigma_A \right)^2 + (\ln(A) \sigma_B)^2 + 2 \frac{B \ln(A)}{A} \sigma_{AB} \right]$$

# Jackknife resampling

- **Definition:** When do jackknife resampling, it takes one data from a sample of  $n$  data each time, and calculates statistics for the remaining data.

- **Estimate:** variance, bias

- **Example:**

Mean:

$$\bar{x}_i = \frac{1}{n-1} \sum_{j \neq i}^n x_j$$

$$D_{(\text{jackknife})} = \frac{n-1}{n} \sum_{i=1}^n (\bar{x}_i - \bar{x}_.)^2$$

# Bootstrapping

- **Definition:** It is a measurement technique based on random repeatable sampling.
- **Estimate:** bias, variance, confidence interval, prediction error
- **Advantage:** very simple. Strong generality, few assumptions(no Gaussian)