

The radial acceleration relation(RAR)
and
baryonic Tully-Fisher relation

Shiyin Shen

[arXiv.1803.01849](https://arxiv.org/abs/1803.01849)

[arXiv.1803.00022](https://arxiv.org/abs/1803.00022)

The radial acceleration relation is a natural consequence of the baryonic Tully-Fisher relation

Coral Wheeler¹★, Philip F. Hopkins¹, Olivier Doré^{1,2}

¹TAPIR, Mailcode 350-17, California Institute of Technology, Pasadena, CA 91125, USA,

²Jet Propulsion Laboratory, 4800 Oak Grove Drive, Pasadena, CA 91109, USA

7 March 2018

ABSTRACT

Galaxies covering several orders of magnitude in stellar mass and a variety of Hubble types have been shown to follow the “Radial Acceleration Relation” (RAR), a relationship between g_{obs} , the observed circular acceleration of the galaxy, and g_{bar} , the acceleration due to the total baryonic mass of the galaxy. For accelerations above 10^{10} m s^{-2} , g_{obs} traces g_{bar} , asymptoting to the 1:1 line. Below this scale, there is a break in the relation such that $g_{\text{obs}} \sim g_{\text{bar}}^{1/2}$. We show that the RAR slope, scatter and the acceleration scale are all natural consequences of the well-known baryonic Tully-Fisher relation (BTFR). We further demonstrate that galaxies with a variety of baryonic and dark matter (DM) profiles and a wide range of dark halo and galaxy properties (well beyond those expected in CDM) lie on the RAR if we simply require that their rotation curves satisfy the BTFR. We explore conditions needed to break this degeneracy: sub-kpc resolved rotation curves inside of “cored” DM-dominated profiles and/or outside $\gg 100$ kpc could lie on BTFR but deviate in the RAR, providing new constraints on DM.

Fitting the Radial Acceleration Relation to Individual SPARC Galaxies

Pengfei Li¹, Federico Lelli^{2,*}, Stacy McGaugh¹, and James Schombert³

¹ Department of Astronomy, Case Western Reserve University, Cleveland, OH 44106, USA
e-mail: pengfeili0606@gmail.com

² European Southern Observatory, Karl-Schwarschild-Strasse 2, Garching bei München, Germany

³ Department of Physics, University of Oregon, Eugene, OR 97403, USA

March 2, 2018

ABSTRACT

Galaxies follow a tight radial acceleration relation (RAR): the acceleration observed at every radius correlates with that expected from the distribution of baryons. We use the Markov Chain Monte Carlo method to fit the mean RAR to 175 individual galaxies in the SPARC database, marginalizing over stellar mass-to-light ratio (Υ_*), galaxy distance, and disk inclination. Acceptable fits with astrophysically reasonable parameters are found for the vast majority of galaxies. The residuals around these fits have an rms scatter of only 0.057 dex ($\sim 13\%$). This is in agreement with the predictions of modified Newtonian dynamics (MOND). We further consider a generalized version of the RAR that, unlike MOND, permits galaxy-to-galaxy variation in the critical acceleration scale. The fits are not improved with this additional freedom: there is no credible indication of variation in the critical acceleration scale. The data are consistent with the action of a single effective force law. The apparent universality of the acceleration scale and the small residual scatter are key to understanding galaxies.

Key words. dark matter — galaxies: kinematics and dynamics — galaxies: spiral — galaxies: dwarf — galaxies: irregular

$$g_{\text{bar}}(R) = (\Upsilon_{\text{disk}} V_{\text{disk}}^2 + \Upsilon_{\text{bul}} V_{\text{bul}}^2 + V_{\text{gas}}^2)/R, \quad (1)$$

where Υ_{disk} and Υ_{bul} are the stellar mass-to-light ratios for the disk and bulge, respectively. Similarly, the observed acceleration can be calculated directly from the observed velocity V_{obs} ,

$$g_{\text{obs}}(R) = \frac{V_{\text{obs}}^2}{R}. \quad (2)$$

According to the RAR (McGaugh 2014; McGaugh et al. 2016; Lelli et al. 2017a), the expected total acceleration g_{tot} strongly correlates with that expected from baryonic distributions g_{bar} ,

- $g_{\text{bar}} < g_{\text{obs}}$ at large radii

$$\text{CDM: } g_{\text{obs}} = g_{\text{tot}} = g_{\text{bar}} + g_{\text{DM}}$$

MOND

$$g_{\text{tot}}(R) = \frac{g_{\text{bar}}}{1 - e^{-\sqrt{g_{\text{bar}}/g_{\dagger}}}}, \quad (3)$$

where $g_{\dagger} = 1.20 \times 10^{-10} \text{ m s}^{-2}$. Thus, one can compare the ob-

- inner region: $g_{\text{bar}} \gg g_{\dagger} : \quad g_{\text{tot}} = g_{\text{bar}}$
- outer region: $g_{\text{bar}} \ll g_{\dagger} : \quad g_{\text{obs}} \approx \sqrt{g_{\text{bar}} g_{\dagger}}$

baryonic Tully-Fisher relation(BTFR)

$M_{\text{bar}} = \mathcal{A} V_f^4$, where V_f is (by definition) measured on the *flat* part of the rotation curve so $V_c(r) \approx V_f$ over a large range of r . If we are

CDM:

- $M_{\text{vir}} = M_{200} = \rho R_{200}^3$
- $V_c^2/R = GM/R^2 \Rightarrow V_c \propto R$
 $\Omega = \text{const}$
- $M_{\text{vir}} \propto V^3$
- $f_b = M_{\text{bar}}/M_{\text{vir}}$ not a constant, $\propto M_{\text{vir}}^{1/3}$

MOND

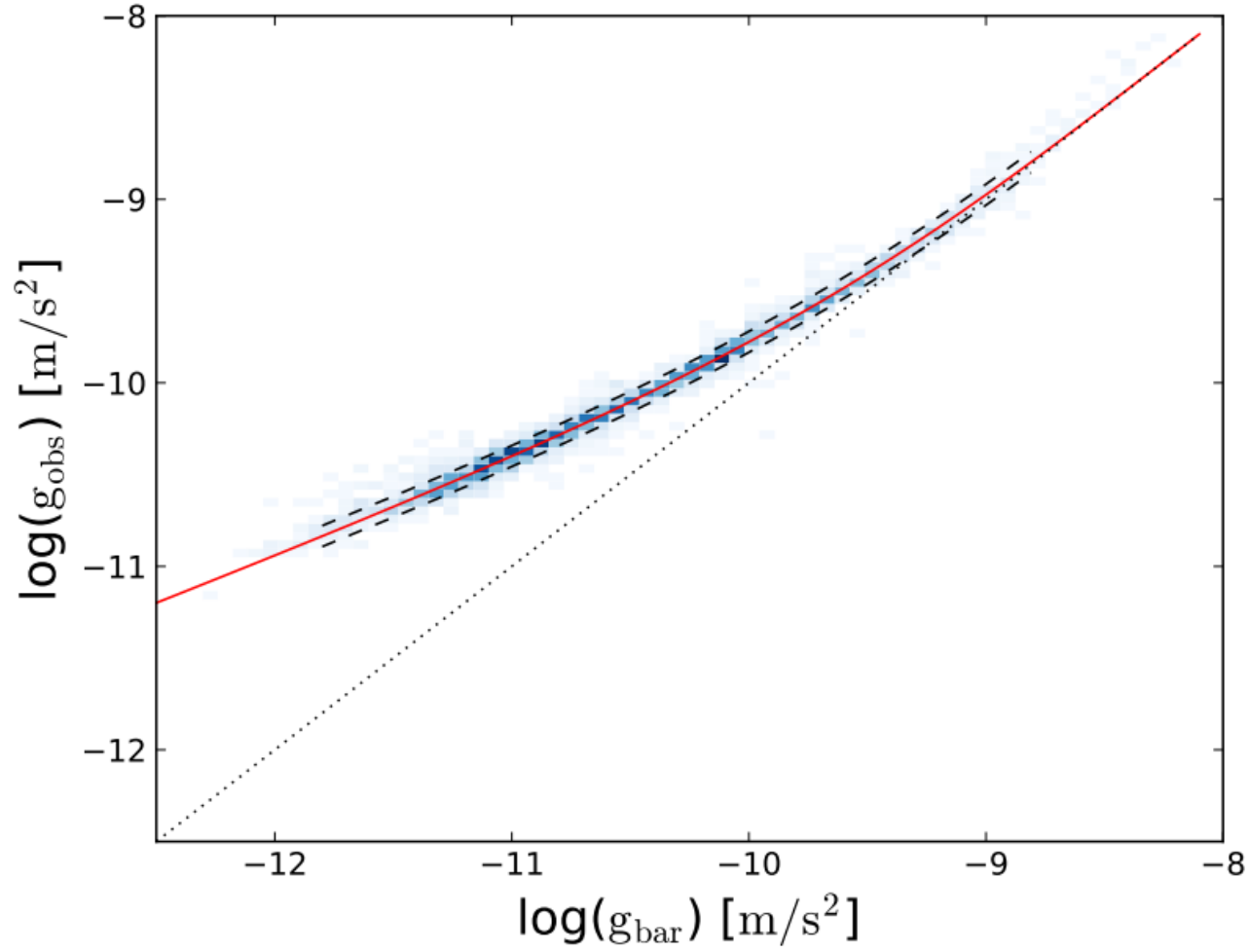
• outer region: $g_{\text{bar}} \ll g_{\dagger}$: $g_{\text{obs}} \approx \sqrt{g_{\text{bar}} g_{\dagger}}$.

• $g_{\text{obs}} = V^2/R$

• $g_{\text{bar}} = M_{\text{bar}}/R^2$

• BTFR is natural conclusion of RAR(MOND)!

MOND VS CDM



Caveats

- $g_{\text{bar}}(R)$: Mass-to-light ratio, distance
- $V(R)$: inclination effect: $\cos i$
- g_+ : if free parameter, can the fitting being improved?

